## Sequential Circuit Synthesis

## Y-0016/004D and 001/2D board (given in next page)

Verfiy JK flip flops with the truth table using Y-0016/004D board for each FF.

## Design Example

Suppose we wish to design a circuit that detects a sequence of three or more consecutive 1's in a string of bits coming through an input line. The input is a serial bit stream.

State diagram


| Present State |  | $\frac{\text { Input }}{x}$ | Next State |  | Output <br> $\boldsymbol{r}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| A | B |  | A | B |  |
| 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 | 0 |
| 1 | 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 | 1 | 0 |
| 1 | 1 | 0 | 0 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 |

Using JK flipflop and its excitation table:

| $\boldsymbol{Q}(\boldsymbol{t})$ | $\boldsymbol{Q}(\boldsymbol{t}+\mathbf{1})$ | $\boldsymbol{J}$ | $\boldsymbol{K}$ |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | X |
| 0 | 1 | 1 | X |
| 1 | 0 | X | 1 |
| 1 | 1 | X | 0 |

(a) $J K$ Flip-Flop

State Table and JK Flip-Flop Inputs

| PresentState |  | $\frac{\text { Input }}{x}$ | Next <br> State |  | Flip-Flop Inputs |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | B |  | A | B | $J_{A}$ | $K_{\text {A }}$ | $J_{B}$ | $K_{B}$ |
| 0 | 0 | 0 | 0 | 0 | 0 | X | 0 | X |
| 0 | 0 | 1 | 0 | 1 | 0 | X | 1 | X |
| 0 | 1 | 0 | 0 | 0 | 0 | X | X | 1 |
| 0 | 1 | 1 | 1 | 0 | 1 | X | X | 1 |
| 1 | 0 | 0 | 0 | 0 | X | 1 | 0 | X |
| 1 | 0 | 1 | 1 | 1 | X | 0 | 1 | X |
| 1 | 1 | 0 | 0 | 0 | X | 1 | X | 1 |
| 1 | 1 | 1 | 1 | 1 | X | 0 | X | 0 |

After filling J, K in the table, Karnough map will be used to simplfy and to find inputs of JK flipflops.

1. A stream of $\mathbf{0}$ 's and $\mathbf{1}$ 's coming from a serial transmission channel. A sequential circuit will be designed that detects 011 sequence coming through this input line.
a. Draw the state diagram.
b. Fill in the state table using JK flipflops
c. Simplify the JKs in Karnough and find their input definitions
d. Implement the circuit using Y-0016/004D board and other necessary gate boards.

