

Instructions: Keep all devices capable of communication turned off and out of sight. **Multiple Choice Questions (44 points)**

Q1 Suppose that $f(x) = |x + 2|$ and the domain of f is $(-\infty, -2]$. Find $f^{-1}(2)$.

- (A) -5 | (C) -2 | (E) None
 (B) -4 | (D) 1

Q2 Let $A = \{a, b, c, d\}$ and $B = \{1, 2\}$ be finite sets. How many functions are there from A to B ?

- (A) 16 | (C) 81 | (E) None
 (B) 32 | (D) 12

Q3 $\lim_{x \rightarrow 0} \frac{\sin x}{\sqrt{x}}$ is

- (A) -1 | (C) 1 | (E) None
 (B) 0 | (D) π

Q4 Suppose $f(x) = \frac{1}{x^2 - 25}$. What is the largest value of A such that $f(x)$ is defined on the interval $[-10, A)$?

- (A) 5 | (C) -2 | (E) None
 (B) $2\sqrt{6}$ | (D) -5

Q5 If $f(x) = |x + 2|$ then find $\lim_{x \rightarrow -2} \frac{f(x) - f(-2)}{x + 2}$

- (A) 4 | (C) 0 | (E) DNE
 (B) 1 | (D) 2

Q6 $\lim_{x \rightarrow 0} \frac{\tan x - x}{\sin x}$ is

- (A) 2 | (C) π | (E) None
 (B) $-\pi/2$ | (D) 0

Q7 $\lim_{x \rightarrow \infty} \frac{5 + 7^x}{2 + 9^x}$

- (A) ∞ | (C) $5/2$ | (E) None
 (B) 0 | (D) $7/9$

Q8 The equation of the slant (or oblique) asymptote to the graph of $f(x) = \frac{x^3 + 1}{x^2 + 1}$ is

- (A) $y = -x$ | (C) $y = -x + 1$ | (E) None
 (B) $y = x + 1$ | (D) $y = x$

Q9 Let $\frac{1}{3}x + \frac{3}{x} + 1 \leq f(x) \leq x^2 - 4x + 6$. Find the $\lim_{x \rightarrow 3} f(x)$

- (A) -1 | (C) 2 | (E) 11
 (B) 0 | (D) 3

Q10 Find the vertical(VA) and horizontal(HA) asymptotes of the function $f(x) = \frac{x^2 + 5x + 6}{x^2 - 4}$.

- (A) $VA : x = \pm 2, HA : y = 1$ | (C) $VA : x = 2, HA : y = 1$
 (B) $VA : x = -2, HA : y = 1$ | (D) None

Q11 $\lim_{x \rightarrow e} [\tan^{-1}(\ln x)]$

- (A) ∞ | (C) $\pi/4$ | (E) None
 (B) π | (D) $-\infty$

True/False questions(16 pts) . No justifications are needed.

Q12 A circle can be the graph of a function.

T | **F**

Q13 If $f(x) = 7 - x + e^{x-2}$. Then $f^{-1}(6) = 2$.

T | **F**

Q14 If $\lim_{x \rightarrow \infty} f(x)$ exists, then $f(x)$ must have a horizontal asymptote.

T | **F**

Q15 If both $f(x)$ and $g(x)$ are odd functions, then their product $f(x)g(x)$ is an even function

T | **F**

Find the following limits. If a limit does not exist, state does not exist and provide a brief explanation. Show all work. No work=No credit(40 pts) .

Q1(20pts) $\lim_{x \rightarrow 0} \frac{\frac{1}{x+7} - \frac{1}{7}}{x}$.

Solution.

Q2(20pts) $\lim_{x \rightarrow 0} \frac{\sin x + 1 - \cos x}{x}$.

Solution.