

Note:Show all work, clearly and in order, if you want to get full credit.

Q1 Let $(1 + x^6)dy = x^5 dx + x^5 y^2 dx$.

1. (5pts) Specify the type of the differential equation.
2. (20pts) Find the general solution.

Solution:

Q2 Let $2xy \frac{dy}{dx} = y^2 - 2x^3$, $y(1) = 2$

1. (5pts) Specify the type of the differential equation.
2. (20pts) Find the solution.

Solution:

Q3 Let $\left[y\left(1 + \frac{1}{x}\right) + \cos y \right] dx + \left[x + \ln x - x \sin y \right] dy = 0$.

1. (5pts) Specify the type of the differential equation.
2. (20pts) Find the solution.

Solution:

Q4 Let $y' + \tan(x)y = \cos^2 x$.

1. (5pts) Specify the type of the differential equation.
2. (20pts) Find the solution.

Solution: